How to get Sol samples?  $_{\rm O}$ 

How best to sample the Sols?  $_{\rm OO}$ 

Processing Sols

Robustness under Risk

# Solution Pluralism, Deliberation, and Metaheuristics

Extracting More Value from Optimization Models Part 2: Engineering and Scientific Challenges.

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http://research.larc.smu.edu.sg/mic2013/

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Outline			



#### How to get Sol samples?







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### Sampling in our examples of part 1

- Philly redistricting project. See cited papers. Basically, OR (IP) heuristic models for initial contiguous solutions, then innovative GA to find high-quality new solutions.
- TSP. Well-known heuristic, Lin 2-opt, with multiple starting points. Lots of obvious alternatives.
- GAP. FI-2Pop GA. Especially good at finding lols [Kimbrough et al., 2008, Kimbrough et al., 2009].
- VRPs. RJR (homegrown, "rotate, jiggle, repair") on top of TSP. Affords multiple solutions.
- 2-sided matching. GAs in multiple cases. ABM in one case [Kimbrough and Kuo, 2010, Kimbrough, 2012].

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Sampling the	Sols		

- Evolutionary computation is a natural place to look first.
- In general, population-based approaches
  - Particle swarm optimization, many forms of EC, ant colony optimization, artificial immune systems, ...
- NB: Interacts with constraint handling.
  - Again, the FI-2Pop GA has been especially good at finding lols [Kimbrough et al., 2008, Kimbrough et al., 2009].

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Points arising			

- Very little is known about which methods of sampling (particularly which metaheuristics) are most effective.
- Conducting local search in the neighborhood of a known (e.g., conventionally discovered) solution is an obvious tactic (but is largely unexplored for these purposes).
- In experiments with GAPs, we found that the Sols (both Fols and lols) were quite dense [Kimbrough et al., 2010].
- Do different sampling methods find very different samples?

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#### How to process large numbers of sampled Sols?

- Reduce by DEA, Pareto dominance.
- DSS. Prototype for GAP-like problems.

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- Standardly: under uncertainty.
- Solution pluralism affords under-risk analyses [Kimbrough et al., 2011].

How to get S o	ol samples?	How best to sample the Sols?	Processing Sols ○	Robustness under Risk ●○
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	Kimbrough, On heuristic marriage pr	S. O. and Kuo, A. (201 cs for two-sided matching oblem as a multiobject	0). ng: Revisiting th ive problem.	e stable

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On using genetic algorithms to support post-solution deliberation in the generalized assignment problem. MIC 2009: The VIII METAHEURISTICS INTERNATIONAL CONFERENCE, conference CD.

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